

## PHYSICAL ANALISE AND CUTTING FORCES IN BEVEL GEAR MACHINING PROCESS

*BOB, Danila*

*UNIO SA Satu Mare - 35, Lucian Blaga Blvd, 3900 Satu Mare, Romania*

[danila.bob@unio.ro](mailto:danila.bob@unio.ro)

***Abstract:** In order to calculate machining forces it is necessary to know the chip volume and the physical model of the bevel gears machining process. It is considered the theory of transfer energy routes and energy quantum applicable to this process. The force variation in time diagram was established.*

***Key words:** bevel gears machining, cutting forces, physical model*

### 1. INTRODUCTION

In the process of bevel gear machining there is a periodically varying chip section during the material removal and the cutting force also varies during this process. Physical analyse and accurate modelling of the cutting forces is required to predict the cutting forces, vibration, surface quality and stability of machining process.

A number of different methods to predict cutting forces have been developed over the last years. These models can be classified into three major categories: empirical, analytical and mechanistic methods [ 1,2,3,4,5]. In the empirical methods, a number of machining experiments are performed and performance measures such as cutting forces, tool life and tool wear are measured. These responses are then correlated to the cutting conditions using empirical functions and require a lot of experimentation. Analytical approaches model the physical mechanisms that occur during cutting. This include complex mechanisms such as high strain rates, high temperature gradients and combined elastic and plastic deformations and it's not yet completely

solved. Mechanistic models predict the cutting forces based on a method that assumed cutting forces to be proportional to the chip cross-sectional area.

The constants of proportionality are called the specific cutting pressures and depend on the cutter geometry, cutting conditions, insert grade and workpiece material properties.

As shown in Figure 1, the cutter turns on its own axis  $O_c$ . As the cutter moves round the rotor axis  $O$ , the gear blank rotates and the cutter will machine the flanks of bevel gear teeth

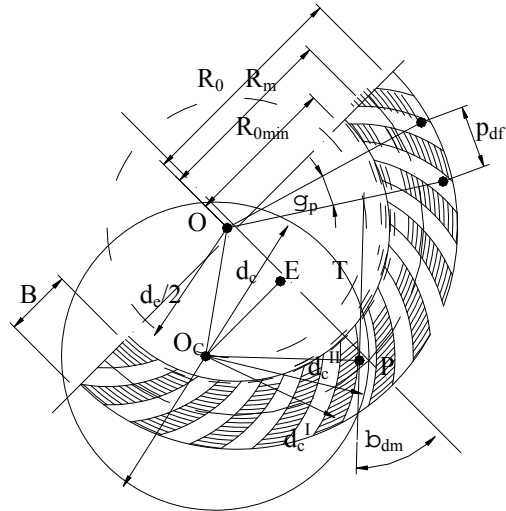


Fig.1. Bevel gear cutting process

The shaded area from Figure 2 is the sectional forms of undeformed chip.

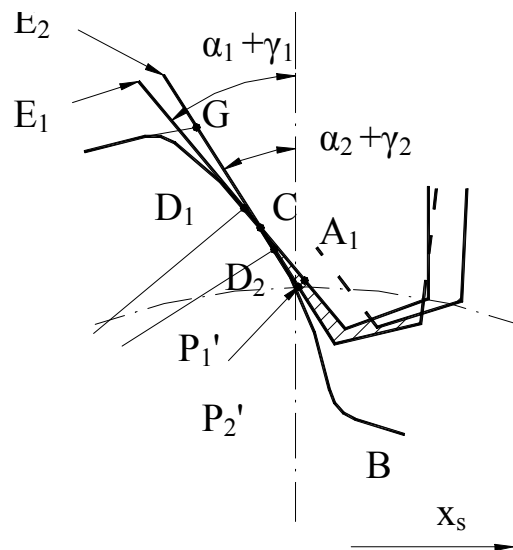


Fig. 2. The sectional of undeformed chip

## 2. MODELING OF PHYSIC WEARING PROCESS OF THE CUTTERS OF THE MILLING HEAD

In order to elaborate a mathematic model of the wear process for the cutters of the milling head for bevel gears, it is considered the set  $N_1$  as the totality of particles of a cutter of the milling head (considered cutter number 1).  $N_1$  consists of a reunion of two complementary subsets  $V_1$  and  $W_1$  [5]:

$$V_1 \cup W_1 = N_1 \quad (1)$$

where:

$V_1$  - contain the particles included in cutter number 1 during the cutting process  
 $W_1$  - contain the particles departed from the cutter number 1 during the cutting process, due to the different forms of the wear process.

It is considered that both the milling head and the cutter where chosen according to the quality of the work material.

It is noted  $V_i$  an element of the set  $V$  and with  $W_i$  the elements of the set  $W$ . A mathematic algorithm can be associated with the wear process of the cutters of the milling head, the correspondence between the phases of the cutting process and the algorithms elements being stated below:

$$V_{10} \cup W_{10} = N_1 \quad (2)$$

for the first interaction tool-working part, and as follows for the next interactions:

$$\begin{aligned} V_{11} \cup W_{11} &= N_1 \\ V_{12} \cup W_{12} &= N_1 \\ V_{13} \cup W_{13} &= N_1 \\ &\vdots \\ V_{1k} \cup W_{1k} &= N_1 \end{aligned} \quad (3)$$

where:

$$V_{11} = V_{10} \cup Z_{11}$$

and  $Z_{11}$  represents all the particles included in the cutters wear quantity for the first interaction tool – part.

It can be also, considered:

$$V_{12} = V_{11} \cup Z_{12} = V_{10} \cup Z_{11} \cup Z_{12} \quad (4)$$

in which  $Z_{12}$  represents all the particles included in the cutter wear quantity for the second interaction tool-part.

$$\begin{aligned}
 V_{13} &= V_{12} \cup Z_{13} = V_{10} \cup Z_{11} \cup Z_{12} \cup z_{13} \\
 V_{14} &= V_{13} \cup Z_{14} = V_{10} \cup Z_{11} \cup Z_{12} \cup Z_{13} \cup Z_{14} \\
 &\vdots \\
 V_{1k} &= V_{1k-1} \cup \dots \cup Z_{1k} = V_{10} \cup Z_{11} \cup Z_{12} \cup Z_{13} \cup \dots \cup Z_{1k}
 \end{aligned} \tag{5}$$

It is then possible to consider the following equation system for the wear of the cutter number 1, which consists of  $N_1$  particles:

$$\begin{aligned}
 Z_{11} &= C_{W_{11}}^{W_{10}} \\
 Z_{12} &= C_{W_{12}}^{W_{11}} \\
 Z_{13} &= C_{W_{13}}^{W_{12}} \\
 &\vdots \\
 Z_{1i} &= C_{W_{1i}}^{W_{1i-1}} \\
 &\vdots \\
 Z_{1k} &= C_{W_{1k}}^{W_{1k-1}}
 \end{aligned} \tag{6}$$

Considering the reunion of the left side members of the equations and the reunion of the right side members of the equations, the result is :

$$Z_{11} \cup Z_{12} \cup Z_{13} \cup Z_{14} \cup \dots \cup Z_{1k} = C_{W_{11}}^{W_{10}} \cup C_{W_{12}}^{W_{11}} \cup C_{W_{13}}^{W_{12}} \cup \dots \cup C_{W_{1k}}^{W_{1k-1}} \tag{7}$$

where:  $Z_{11} \cup Z_{12} \cup Z_{13} \cup Z_{14} \cup \dots \cup Z_{1k} = W_{1k}$  (8)

Because :  $W_{1k} = C_{N_1}^{V_{1k}}$  , (9)

the equation (4.) can be written as:

$$\bigcup_{1(1,1,\dots,k)} C_{W_{1i}}^{W_{1i-1}} = C_{N_1}^{V_{1k}} \tag{10}$$

where:

$C_{W_{1i}}^{W_{1i-1}}$  is the complement of the set  $W_{1, i-1}$  reported to the set of particles  $W_i$

$C_{N_1}^{V_{1k}}$  is the complementary set of the set  $V_{1k}$  reported to the set of particles  $N_1$

The equation (10) represents the general equation of the wearing process of a cutter from the milling head (number 1). The milling head has n cutters which wear during the cutting process.

Generalizing, the following is obtained [5]:

$$\begin{aligned}
 \bigcup_{1(1,1,\dots,k)} C_{W_{1i}}^{W_{1i-1}} &= C_{N_1}^{V_{1k}} \\
 \bigcup_{1(1,2,\dots,k)} C_{W_{2i}}^{W_{2i-1}} &= C_{N_2}^{V_{2k}} \\
 &\vdots \\
 \bigcup_{1(1,1,\dots,k)} C_{W_{ni}}^{W_{ni-1}} &= C_{N_1}^{V_{1k}}
 \end{aligned} \tag{11}$$

These equations represent the equation system which can be considered as a mathematic model of the wearing process for one cutter of the milling head.

### 3. CUTTING FORCES IN BEVEL GEAR MACHINING PROCESS

We consider that the technological system consist from  $M_1$  particles (  $M$  particles being cutting piece) and also that the force is a result of the energy introduced in the process by cutting piece[5]. We admit also that the group of the particles from the process wich receive energy, will transmit this energy to the neighbouring particles.

It is considered  $k$  transfer energy routes coresponding to each energy quantum. Different forms of energy are conducted on the same routes: heat, light, noise. For each route it is possible to associate a work function  $f_i$ , wich can take the value  $a_i$ , where  $a$  is 0 (if at the end of the route energy  $E_i = 0$ ) or 1 (if  $E_i \neq 0$ ),  $E_i$  being energy quantum wich follows  $i$  route.

It is possible to write for each collision the totality of work function. For the first collision:

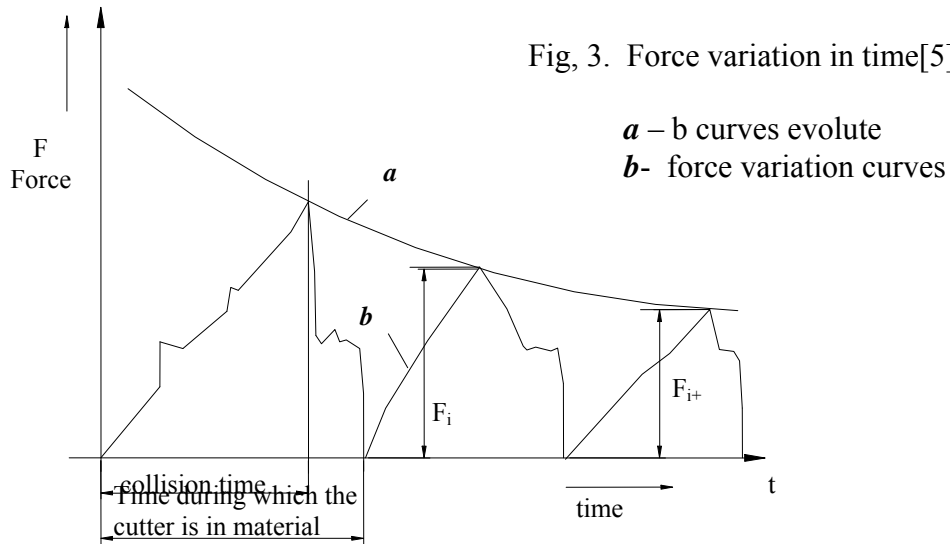
$$F_1 \left\{ \begin{aligned} f_{11}(a_{1n_1}, a_{1n_1-1}, \dots, a_{12}, a_{11}) &= \alpha_{11} \\ f_{12}(a_{2n_2}, a_{2n_2-1}, \dots, a_{22}, a_{21}) &= \alpha_{12} \\ f_{1K}(a_{Kn_k}, a_{kn_k-1}, \dots, a_{k2}, a_{k1}) &= \alpha_{1k} \end{aligned} \right. \tag{12}$$

where:  $\Sigma(a_{in_1}, a_{in_2}, \dots, a_{in_k}) = M$ . The totality  $M$  of the particles decrease as a result of the first collision. Will remain into the process  $M'$  particles and the work function for each route will be modified.

It is possible to write the totality of work function for the second collision and for the followings. For the  $\eta-1$  collision ( $\eta$  is the number of the tool collision necessary for a complete machining) the work function are:

$$F_{\eta-1} \begin{cases} f_{\eta-1,1}(a_{1n_1}, a_{1n_1-1}) = \alpha_{\eta-1,1} \\ f_{\eta-1,2}(a_{2n_2}, a_{2n_2-1}) = \alpha_{\eta-1,2} \\ f_{\eta-1,k}(a_{kn_k}, a_{kn_k-1}) = \alpha_{\eta-1,k} \end{cases} \quad (13)$$

Equations (10) and (13) can be represented by the theoretical diagram from figure 3 .



#### 4.CONCLUSIONS

On these basis it is possible to develop the study of cutting forces in the definitely conditions of bevel gears machining process.

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